

Time-of-Flight PET using Cherenkov Photons Produced in PbF₂ Crystals

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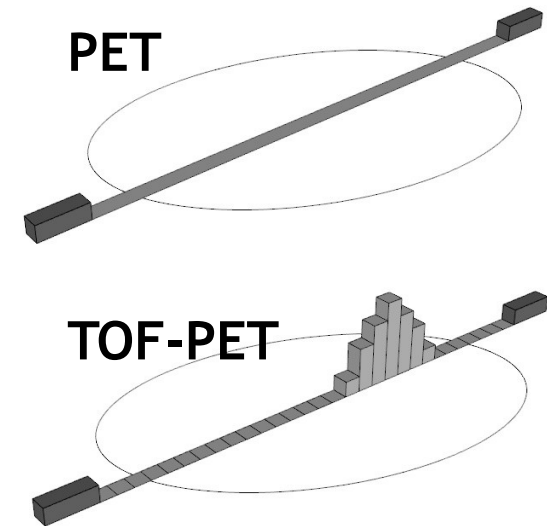
Outline:

- detection method & Cherenkov radiator
- MCP PMT & experimental setup
- simulations
- back-to-back timing resolution
- summary

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TOF PET using Cherenkov photons

- Contrast of images obtained with positron emission tomography (PET) can be improved by measuring time-of-flight (TOF) difference of annihilation gammas
 - localizes source position on line of response (LOR)
 - reduces number of background sources on LOR contributing to random coincidences
 - improves S/N ratio



- Novel photon detectors (SiPM, MCP-PMT) have excellent timing resolution → time-of-flight resolution is limited by scintillation decay time.
- Charged particles passing through matter at a speed higher than the speed of light ($v_{\text{Thr}} > c_0/n$) produce prompt Cherenkov photons.
- However, at low energies (e^- from 511 keV annihilation γ), only a small number of Cherenkov photons is produced → single photon detection.

Cherenkov radiators

- To obtain Cherenkov photons from 511 keV annihilation gammas, they must transfer their energy to an electron in a suitable Cherenkov radiator:
 - high 511 keV γ stopping power \rightarrow high ρ/Z
 - high fraction of γ interactions via photoeffect - electron receives more energy than via Compton scattering \rightarrow high Z
 - high enough index of refraction - more electrons produced above Cherenkov threshold v_{Thr}
 - good optical properties - transmission for visible & near UV Cherenkov photons
- Most promising available crystals: PbF_2 and PbWO_4 (PWO)

	ρ (g/cm ³)	n ($\lambda=400\text{nm}$)	E_{Thr} (keV) for e^-	Optical transmission λ_{Cutoff} (nm)	Light yield (ph/MeV)	Decay time (ns)	Emission peak (nm)
PbF_2	7.77	1.8	104	250	-	-	-
PbWO_4	8.28	2.3	56	350	200	6 / 30	440 / 530

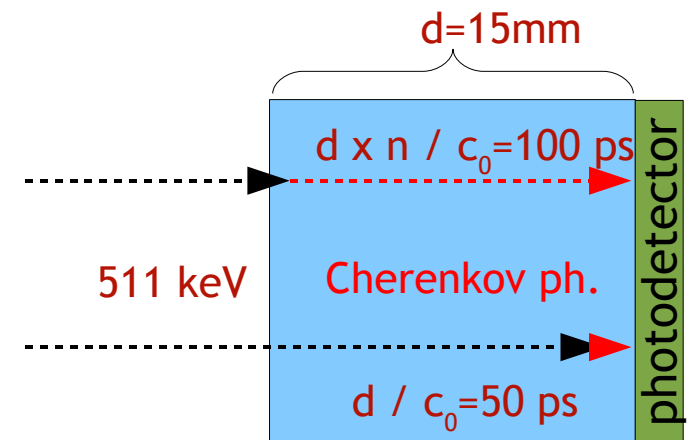
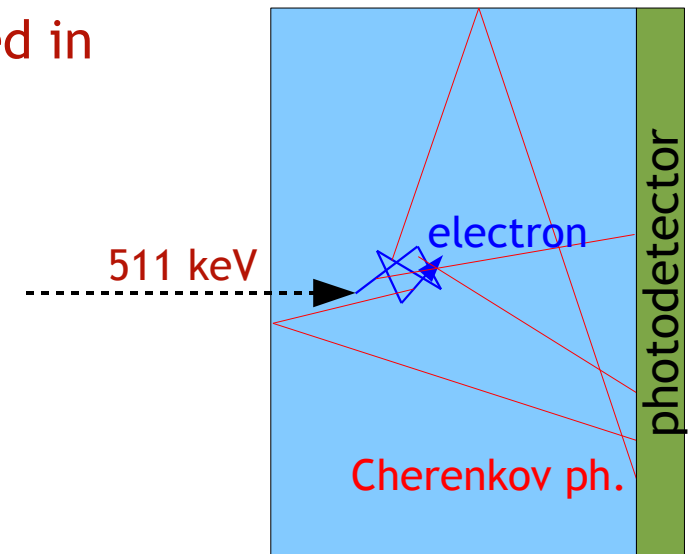
Cherenkov photon production

- Estimated number of Cherenkov photons produced in 15mm thick crystal with $n=2.0$, assuming e^- path length of $l=100\mu\text{m}$ and Cherenkov photon energy interval of 3eV ($\sim 250 - 700\text{nm}$):

$$N \approx 370 (\text{eV}^{-1} \text{cm}^{-1}) \cdot l \cdot \Delta E \cdot \sin^2\theta_c$$

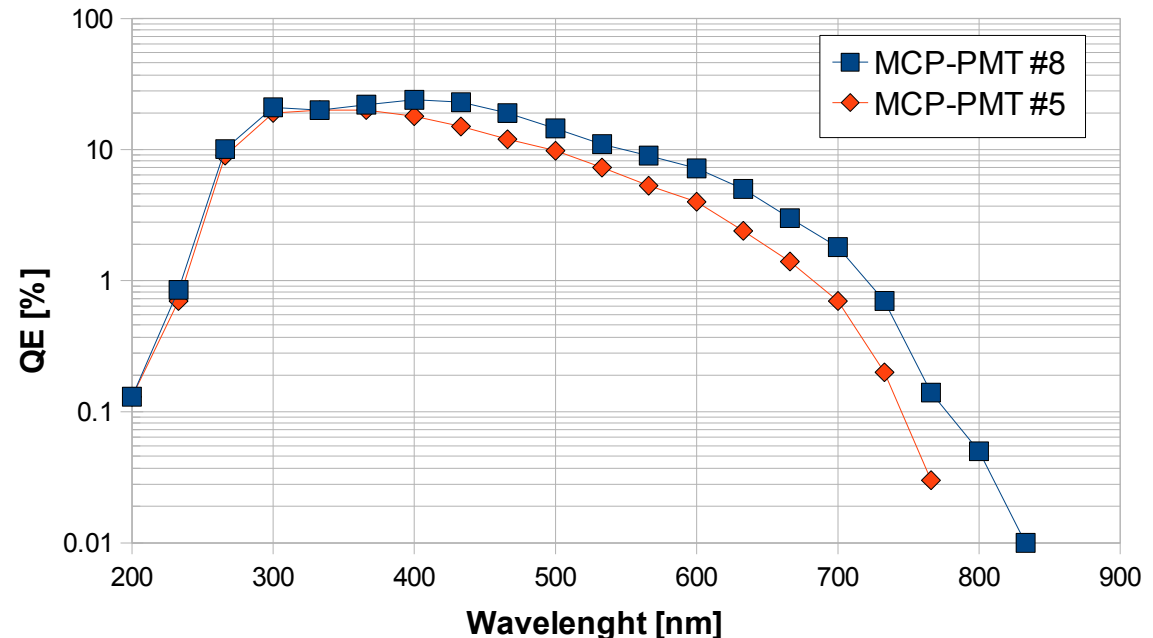
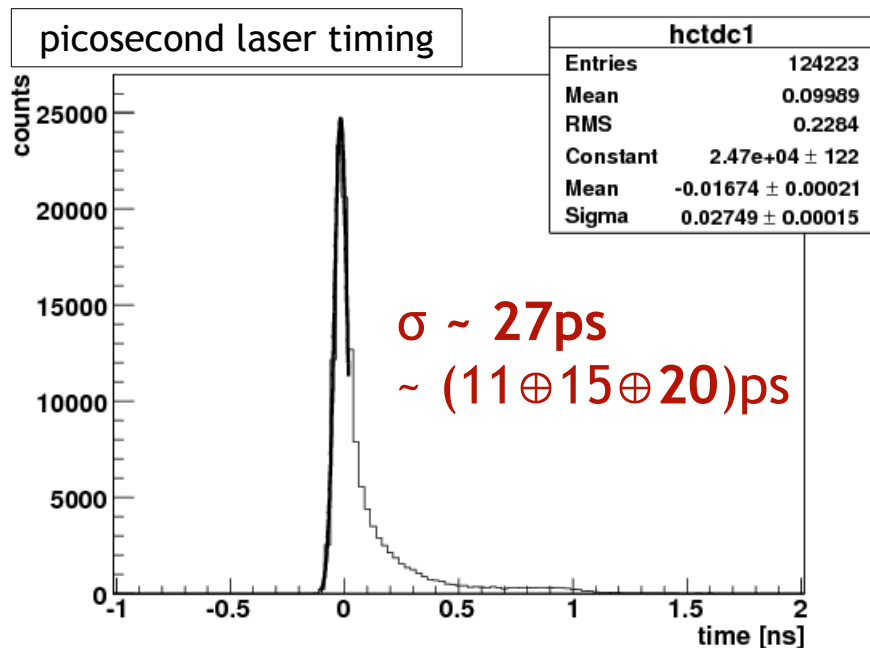
$$N \approx 370 \cdot 0.01 \cdot 3 \cdot 0.75 \approx 8$$

- optical photon travel time in the crystal a significant contribution to the timing resolution
 - even for Cherenkov photons going straight to the photodetector the time spread of 50 ps results from depth of interaction
 - additional variations due to initial path direction, reflections



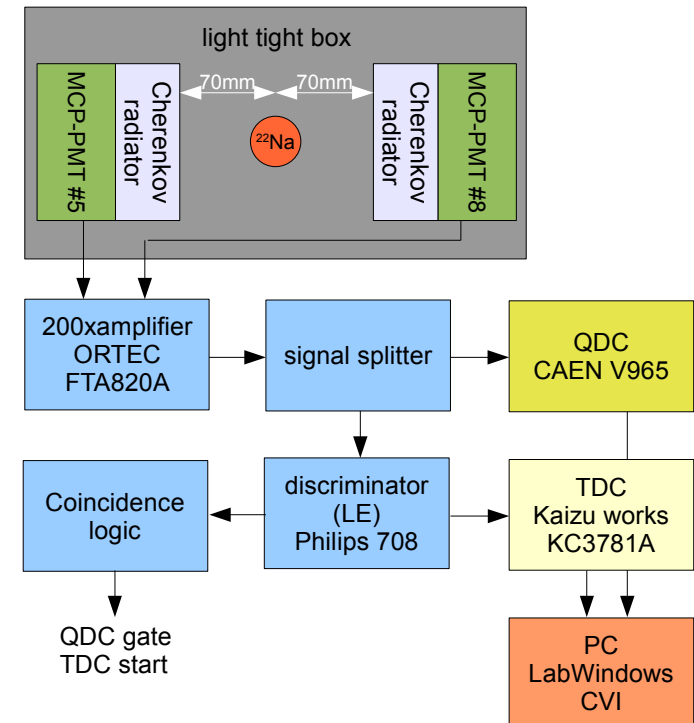
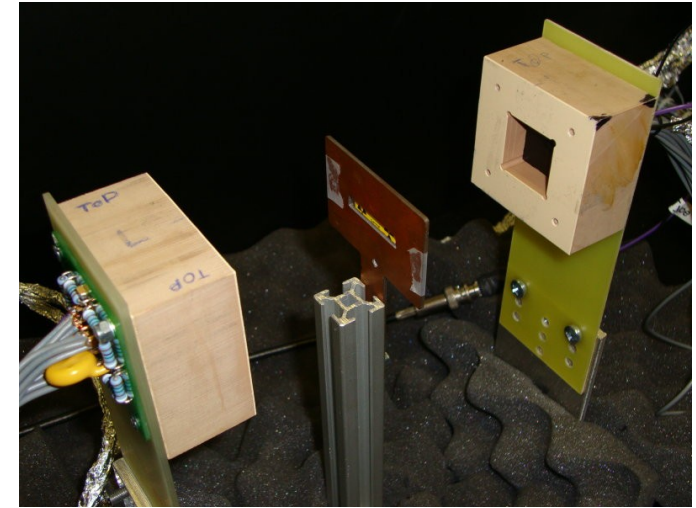
Microchannel plate photomultipliers

- two Hamamatsu MCP PMTs (prototypes for Belle II TOP counter), #5 and #8
 - PMT with two MCP steps, 10 μ m pores
 - multi-anode, 16 (4x4) pads, pitch ~ 5.575mm
 - active surface 22.5x22.5mm²
 - multi-alkali photocathode, 1.5mm thick borosilicate window
 - excellent timing $\sigma \sim 20$ ps for single photons



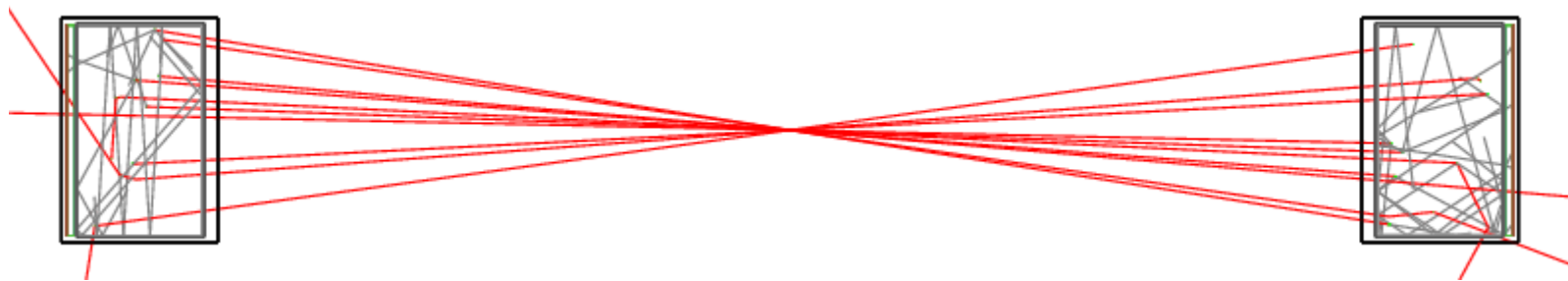
Experimental setup

- Two detectors in back-to-back configuration
 - 25x25x15 (5) mm³ PbF₂ or PbWO₄ crystals, coupled to MCP-PMT with optical grease
 - ²²Na point source
- Readout
 - amplifier (ORTEC FTA820)
 - LE discriminator (Philips sc. 708)
 - TDC (25ps/bin Kaizu works KC3781A)
 - QDC (CAEN V965)
 - time-walk correction applied in analysis



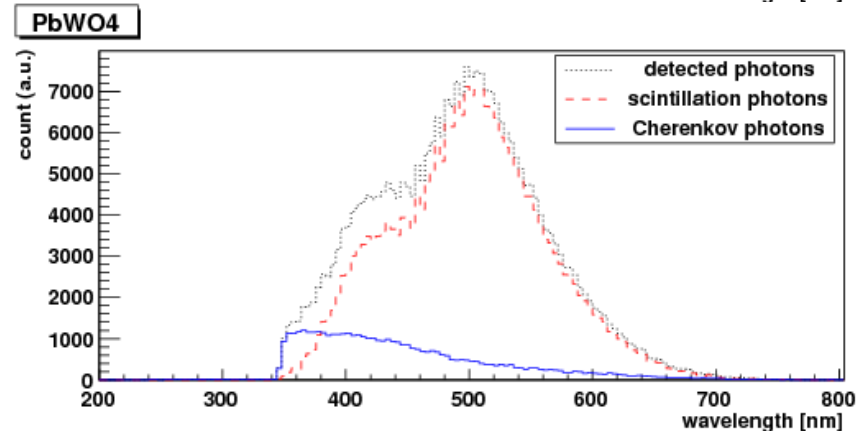
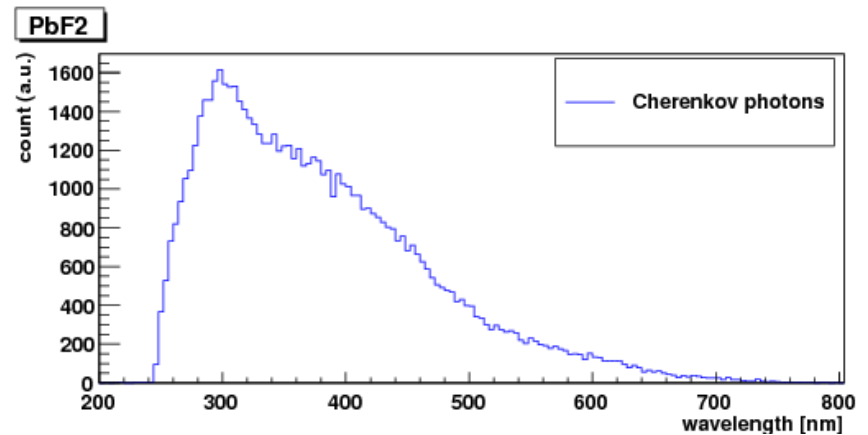
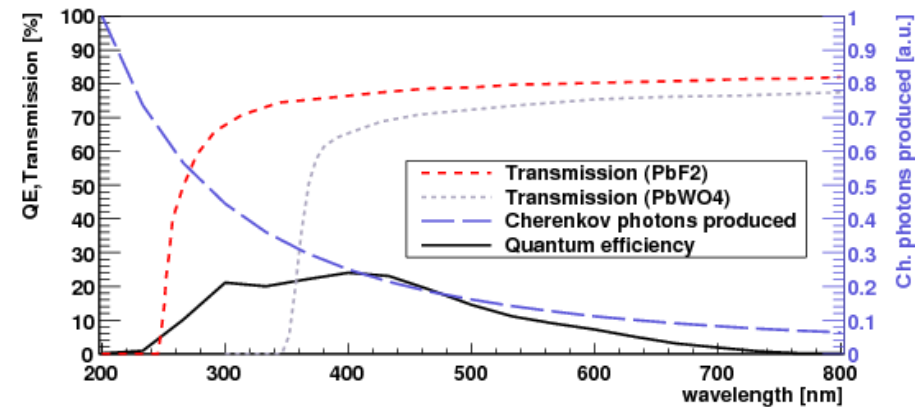
Simulation

- experimental back-to-back configuration was simulated in GEANT4, taking into account:
 - 511keV gamma pairs interacting with the crystals
 - optical photons produced between 250nm - 800nm by Cherenkov process (and scintillation in case of PbWO_4)
 - optical photon boundary processes (exit surface polished, other surfaces polished and wrapped in diffuse reflector - Teflon or painted black)
 - 1.5mm borosilicate photodetector window, coupled with optical grease ($n=1.5$)
 - photodetector QE
 - perfect photodetector timing - simulated timing resolution only includes photon travel time spread



Simulation - Optical photon production

- wavelength distributions for number of Cherenkov photons produced, QE and optical transmissions
- wavelength distributions of first detected photon (Cherenkov or scintillation)
- more Cherenkov photons produced in PbWO_4 , however due to worse transmission less are detected than in PbF_2

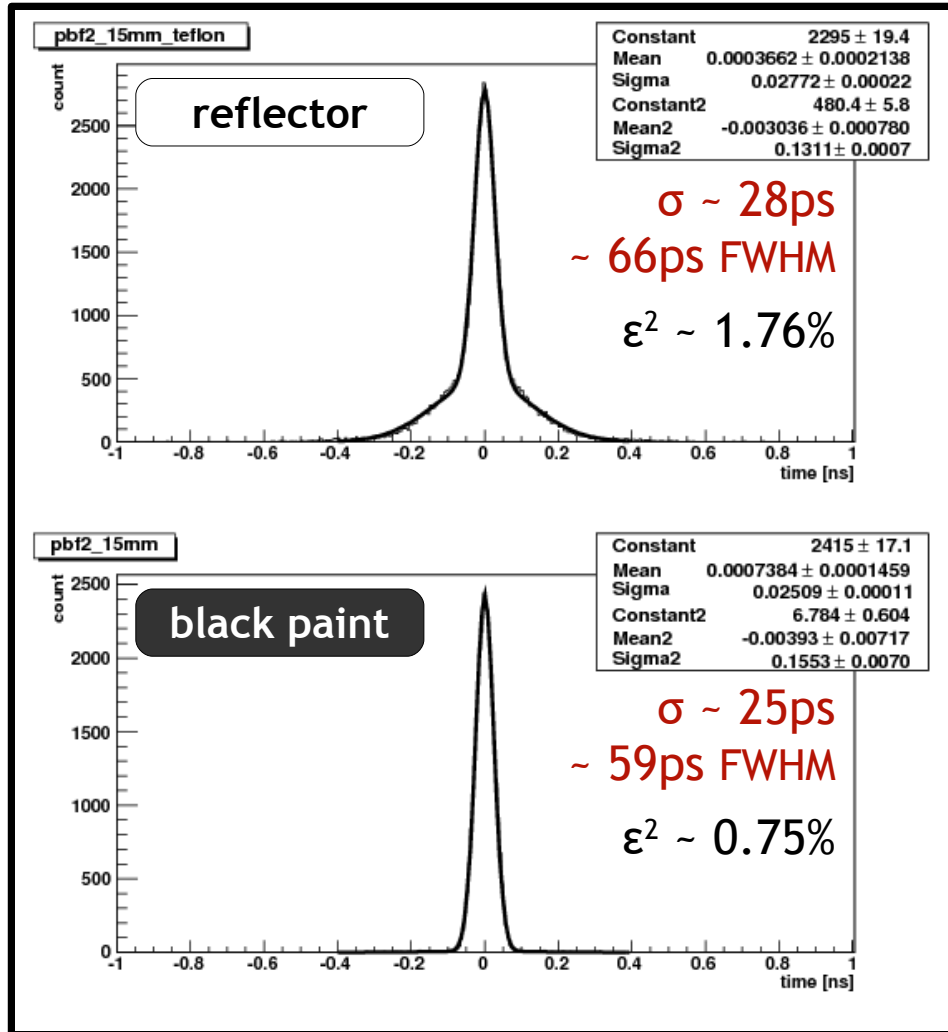


	PbF_2	PbWO_4
e^- above E_{Thr}	77%	88%
Ch.ph. produced / γ	10.2	15.8
Ch.ph. detected / γ (reflector)	0.11	0.68
Ch.ph. detected / γ (black paint)	0.070	0.044

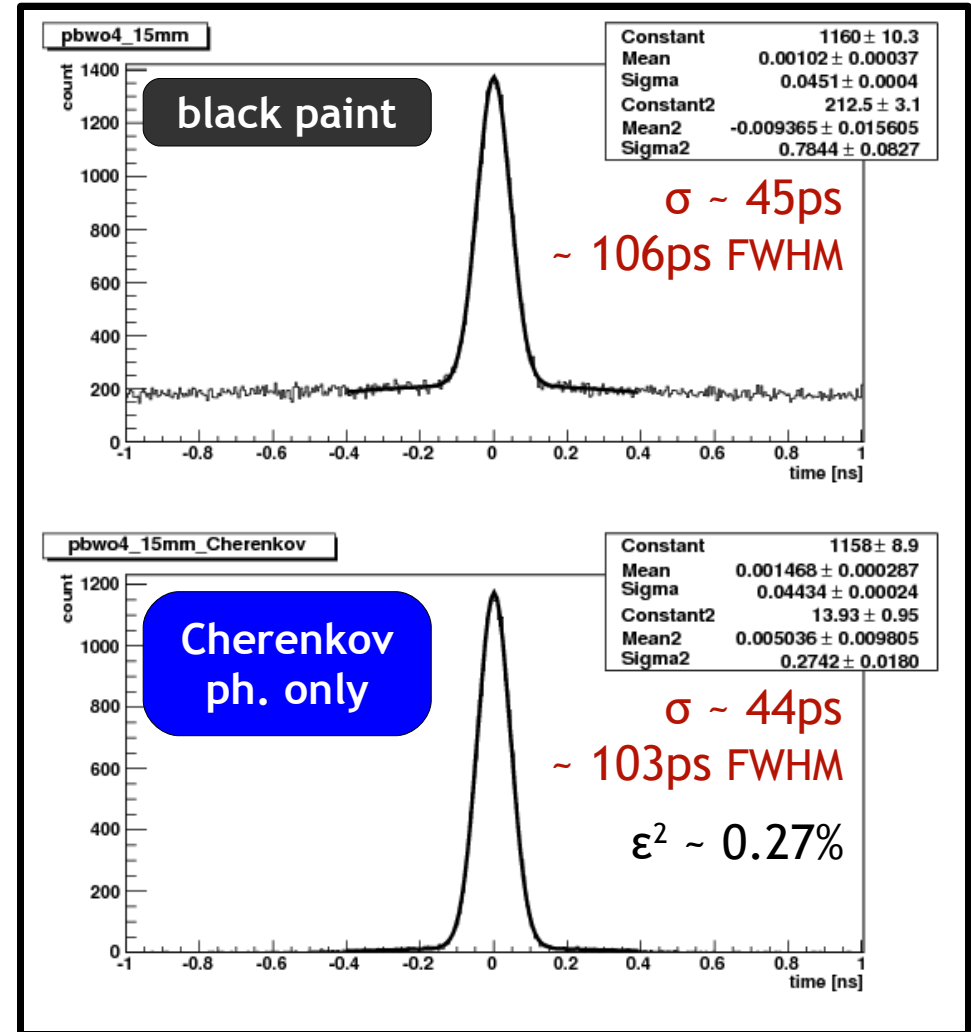
Simulation - coincidence timing resolution and efficiency (ϵ^2)

- time difference between first optical photons reaching each photodetector

PbF₂



PbWO₄



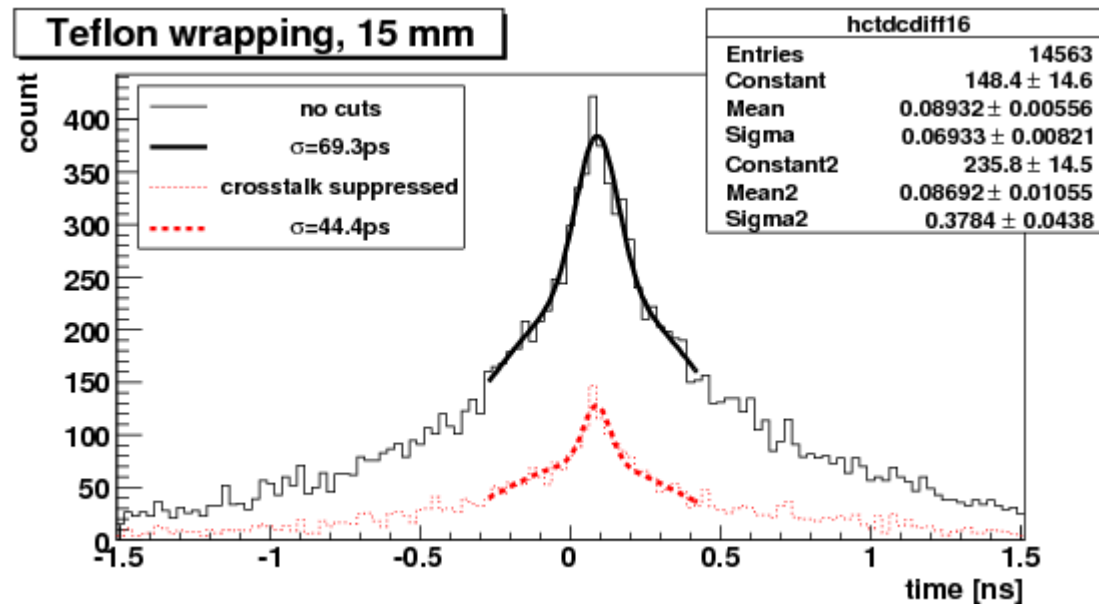
Simulation - summary

- detection of single photons & QE - very low coincidence efficiency (~ 1%)
- black paint stops most reflections at crystal surfaces
 - improves timing
 - reduces efficiency (but mostly at the expense of photons with bad timing)
- PbF_2
 - expected coincidence resolution $\sigma \sim (25 \oplus 2 \cdot 20) \text{ps} \sim 40 \text{ps}$ (15mm thick, black painted crystals)
- PbWO_4
 - higher $\rho \rightarrow$ gamma stopping power
 - higher n and $Z \rightarrow$ more e^- above Ch. threshold \rightarrow more Ch. photons
 - optical transmission λ_{Cutoff} \rightarrow less Cherenkov photons detected
 - higher $n \rightarrow$ slower optical photons \rightarrow worse timing resolution
 - scintillation background



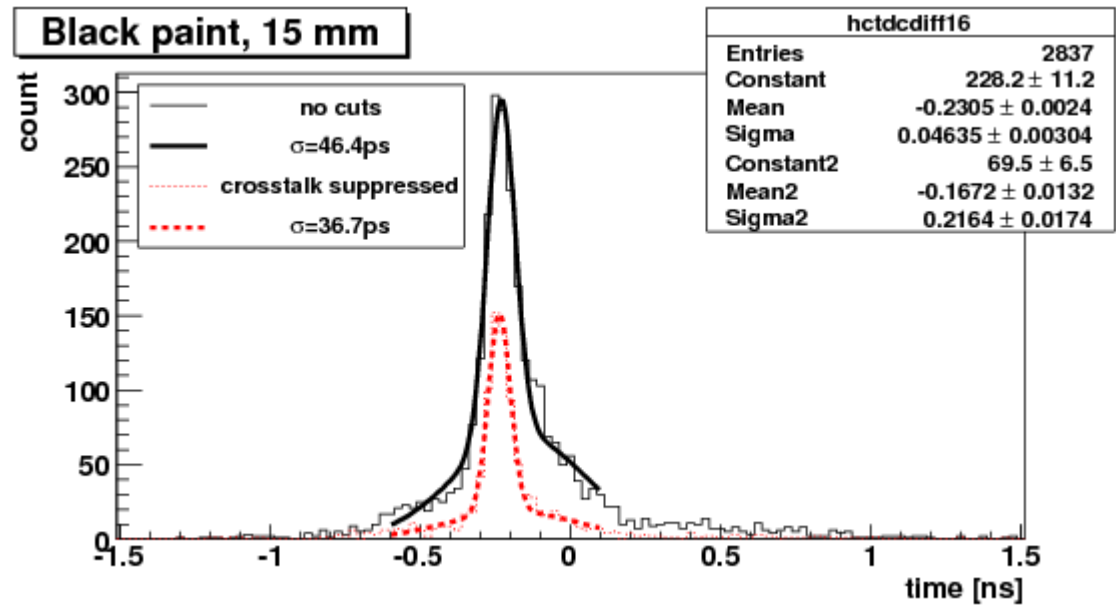
Experimental results - coincidence timing resolution

- time-walk corrected time difference between two selected channels, located near the center of MCP PMT
- crosstalk suppressed events - only events, where the selected channels had maximum charge on their MCP PMT
- 15mm thick PbF_2 crystals, wrapped in Teflon: $\sigma \sim 44\text{ps}$ (103ps FWHM)
 - reflected photons are significantly delayed and produce long tails

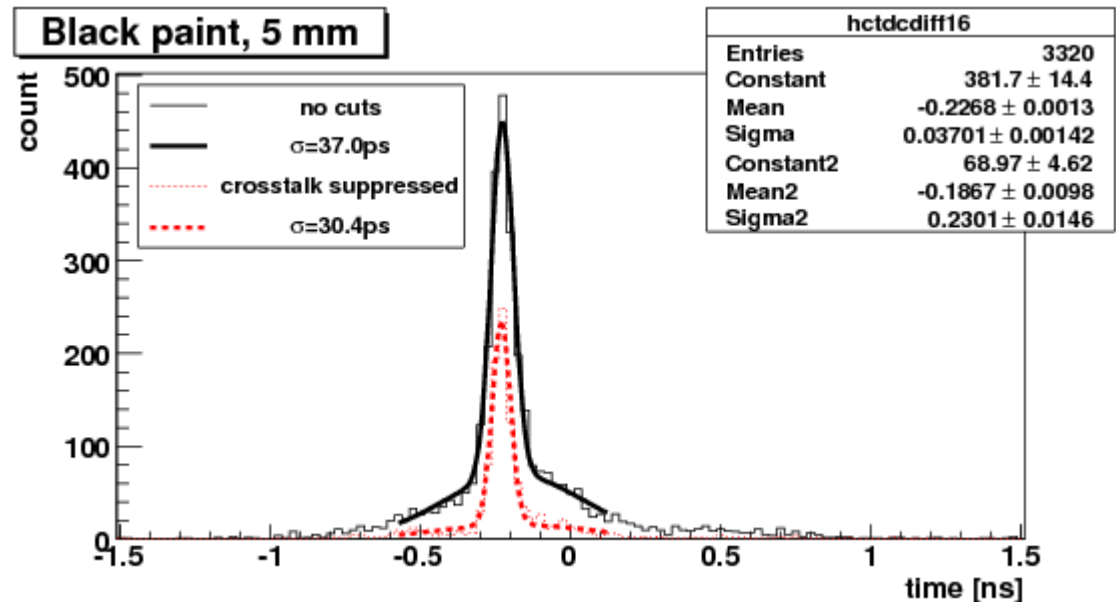


Experimental results - coincidence timing resolution

- black painted, 15mm thick PbF₂ crystals: $\sigma \sim 37\text{ps}$ (87ps FWHM)



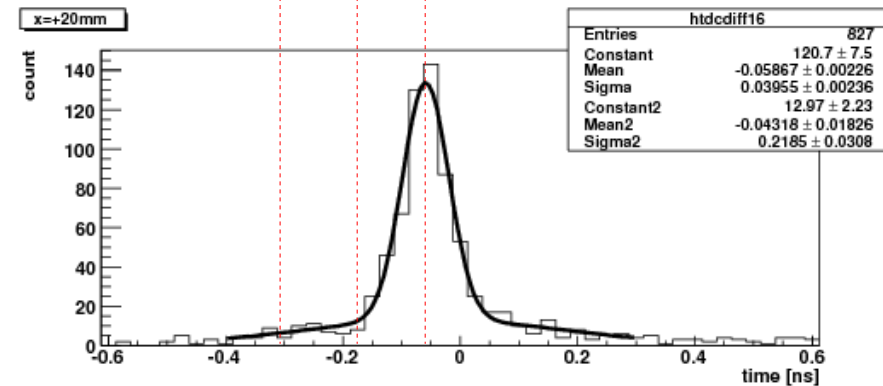
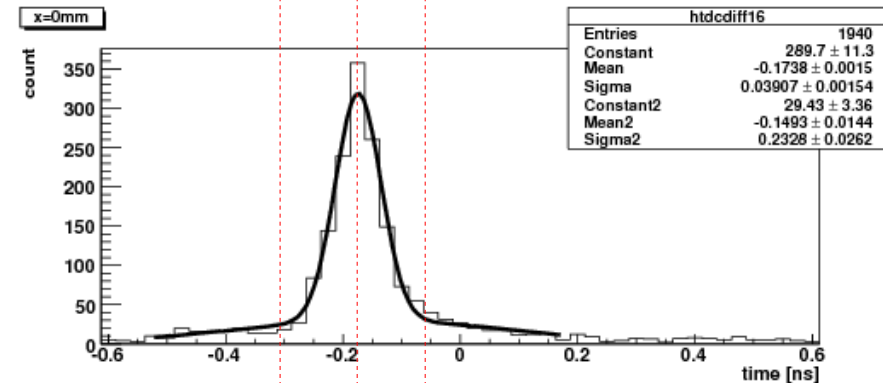
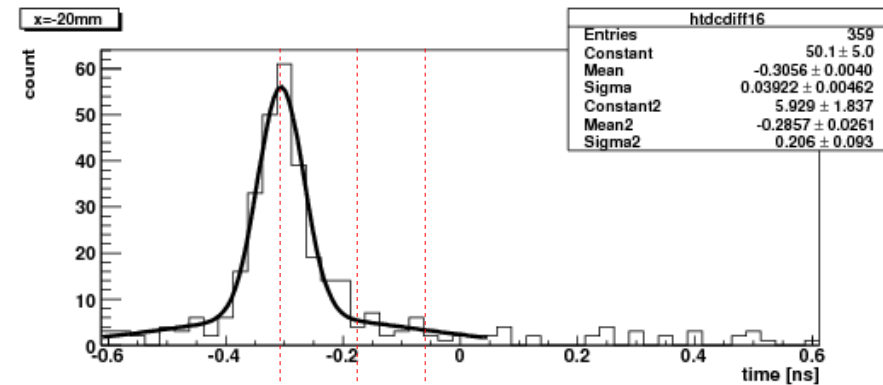
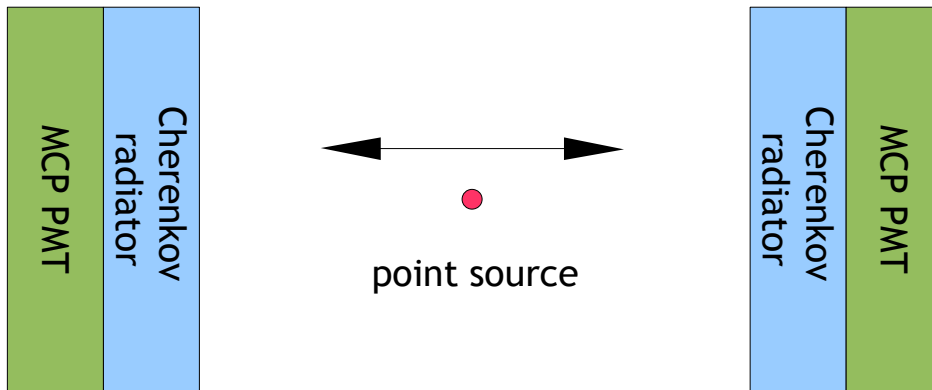
- black painted, 5mm thick PbF₂ crystals: $\sigma \sim 30\text{ps}$ (71ps FWHM)



Experimental results - point source position

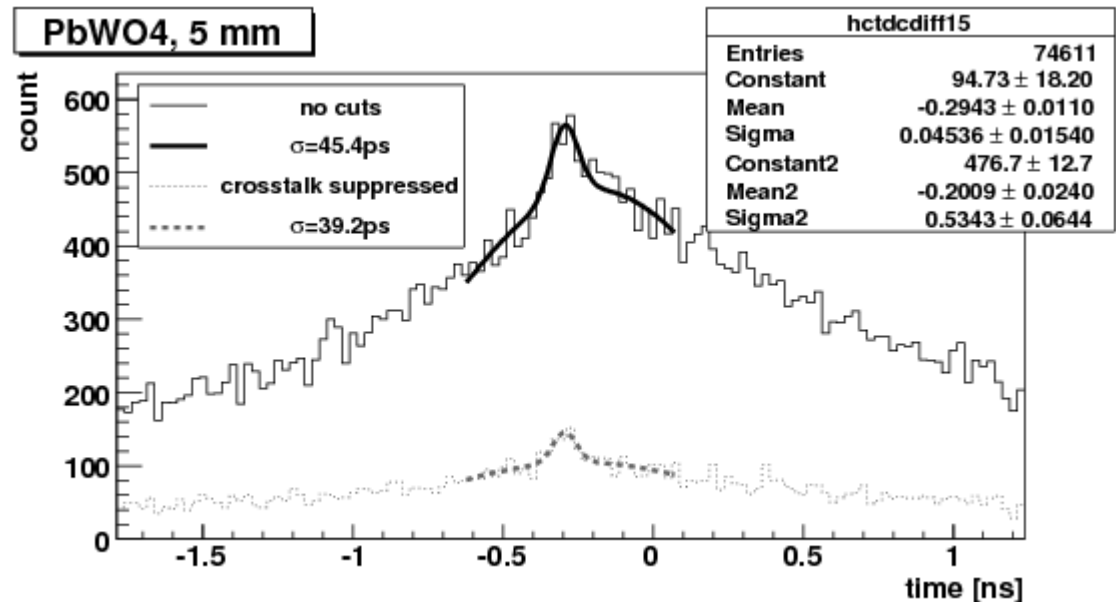
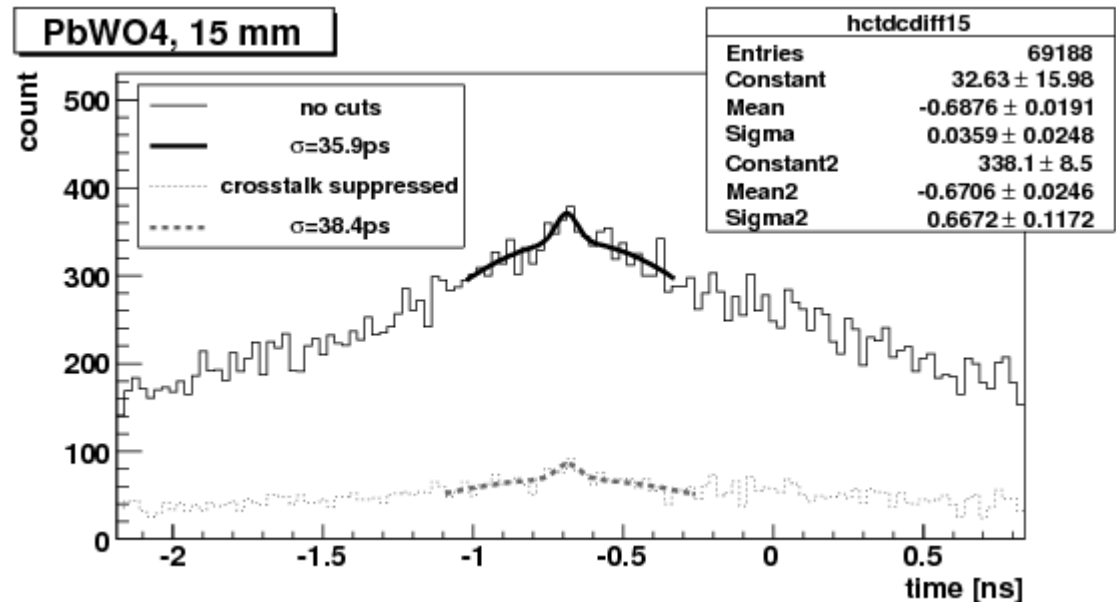
- black painted, 15mm thick PbF_2 crystals
 - point source moved in 20mm steps along LOR
 - average time shift $\sim 125\text{ps}$ ($\rightarrow 19\text{mm}$)
 - timing resolution $\sigma \sim 40\text{ps}$
- \rightarrow position resolution $\sigma \sim 6\text{mm}$ (14mm FWHM)

$$\Delta x = \frac{c_0 \Delta t}{2}$$



Experimental results - PbWO₄

- black painted, 15mm & 5mm thick PbWO₄ crystals
- narrow (Cherenkov) peak barely visible, even at 5mm
- 15mm: $\sigma \sim (38 \pm 18)$ ps
- 5mm: $\sigma \sim (39 \pm 10)$ ps
- majority of events produced by single photon detection
- coincidence rate ~ 30 x the rate with PbF₂ crystal (15mm thickness) \rightarrow majority of events produced by scintillation



Summary

- Scintillation decay limits the TOF resolution
- Prompt Cherenkov photons in combination with very fast photodetectors can be used to measure TOF for 511keV annihilation gammas
- The limiting factor becomes the propagation time spread of Cherenkov photons in the crystal
- Measured coincidence time resolution for
 - 5mm thick PbF_2 crystal $\sigma \sim 30\text{ps}$ (71ps FWHM)
 - 15mm thick PbF_2 crystal $\sigma \sim 37\text{ps}$ (87ps FWHM)
- Measured position resolution along LOR $\sigma \sim 6\text{mm}$ (14mm FWHM)
- With PbWO_4 crystal the scintillations present a challenge
- Efficiency of this method is rather low ($\sim 1\%$)
 - improvements possible with SBA photocathode, quartz PMT window and possible new Cherenkov radiators (transmission in UV)
 - such excellent time resolution may enable modified reconstruction methods, maybe possible with lower statistics

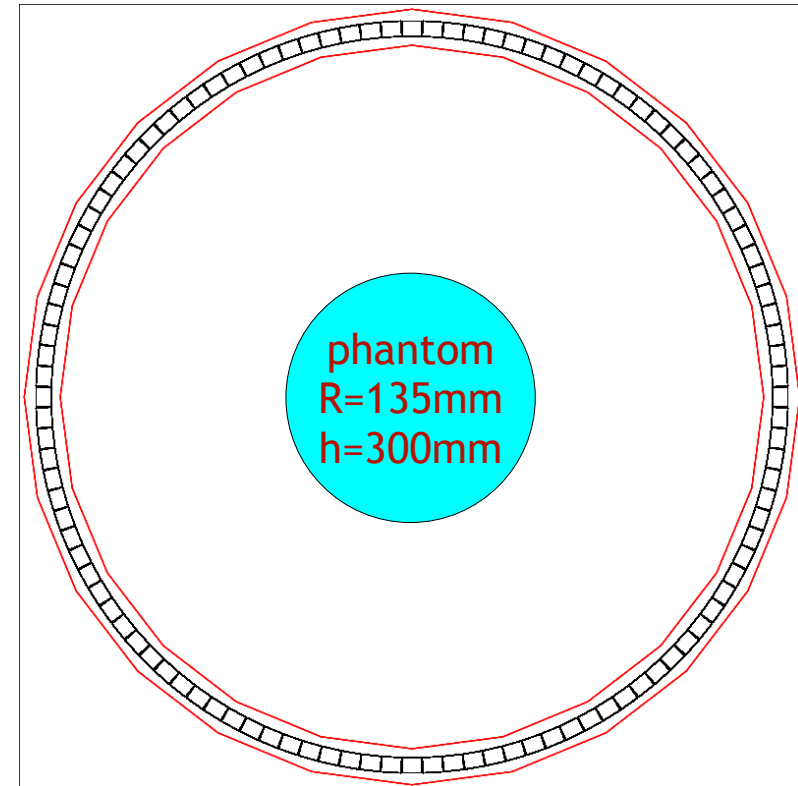
Backup slides

Reconstruction - first attempt

- simulated full body scanner:
 - 16 rings (~370mm axial coverage)
 - ring R=400mm, 112 detectors/ring
 - detector: 15mm thick, black painted PbF₂, segmented into 4x4 (~5.5mm pitch)
 - MCP PMT time response included
- phantom R=135mm, h=300mm
- 2 point (R=0.3mm) sources
 - at (-5,-5,-5) mm and (5,5,5) mm
- Most Likely Position reconstruction method
 - point on LOR defined by TOF information

$$r = \frac{(r_1 + r_2)}{2} - \frac{c_0 \Delta t (r_2 - r_1)}{d_{LOR}}$$

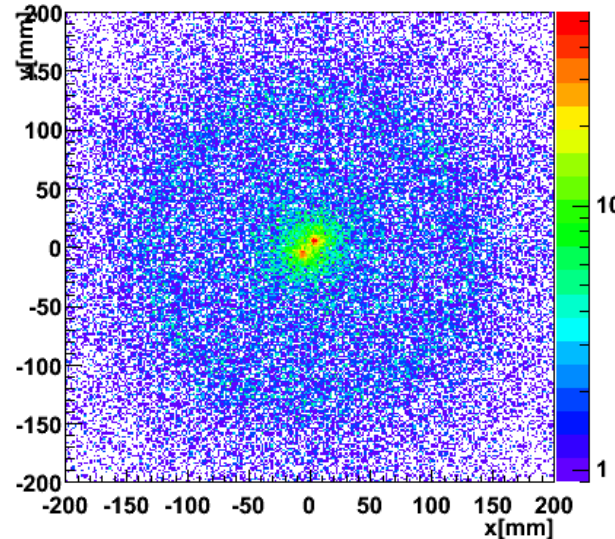
- deconvoluted by Gaussian response function ($\sigma = 20\text{ps} \rightarrow 3\text{mm}$)



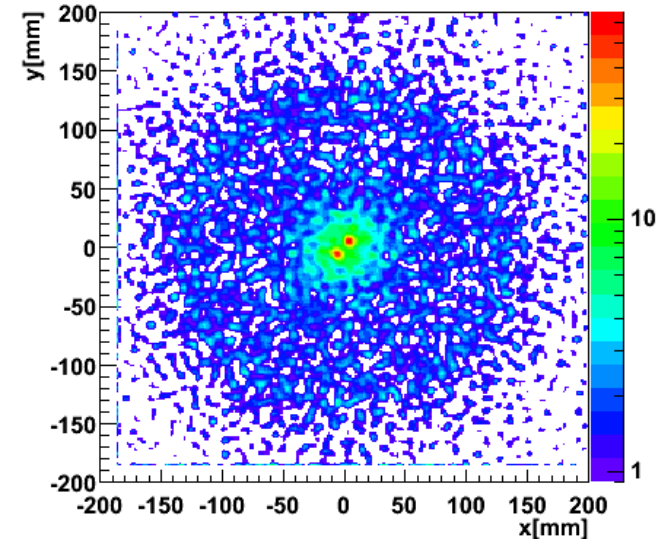
Reconstruction - MLP method

- transverse projection
- all coincidences, including all crossplane
- phantom visible
- two sources separated by $\sim 14\text{mm}$ in projection

Simulated events

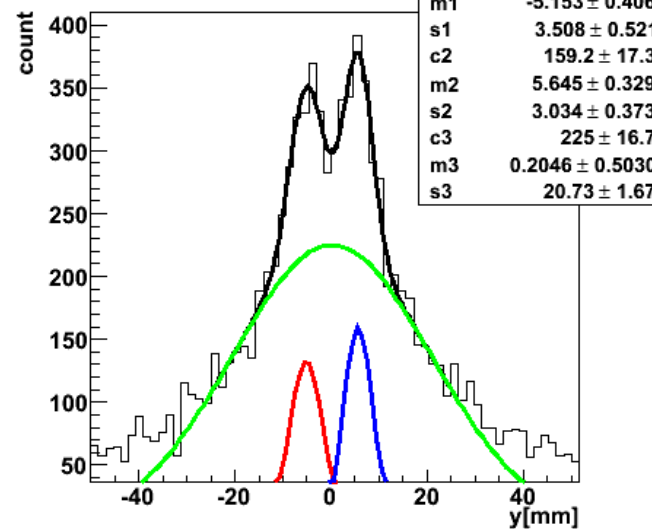


Deconvolution

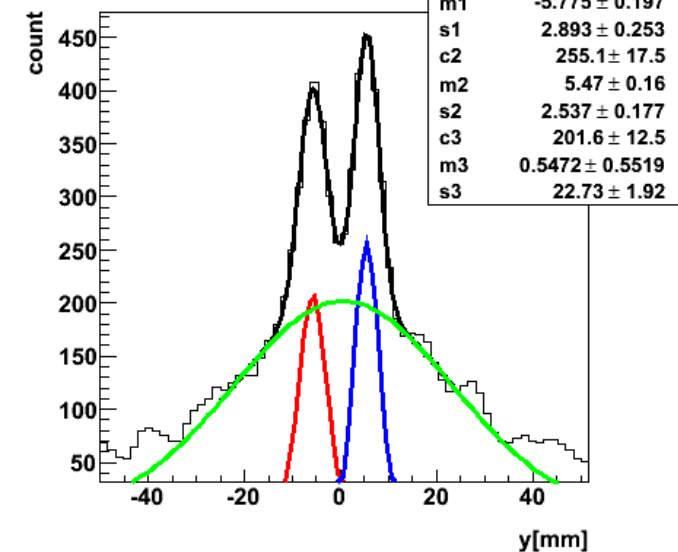


- 1D projection along Y
 - $\sigma \sim 3.5\text{mm}$
- after deconvolution
 - $\sigma \sim 2.9\text{mm}$

Simulated events

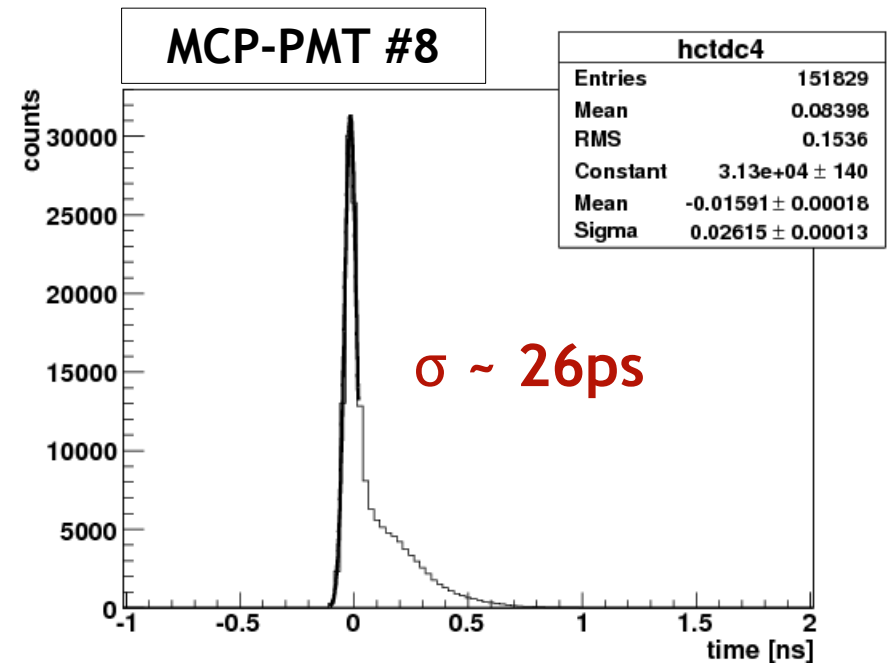
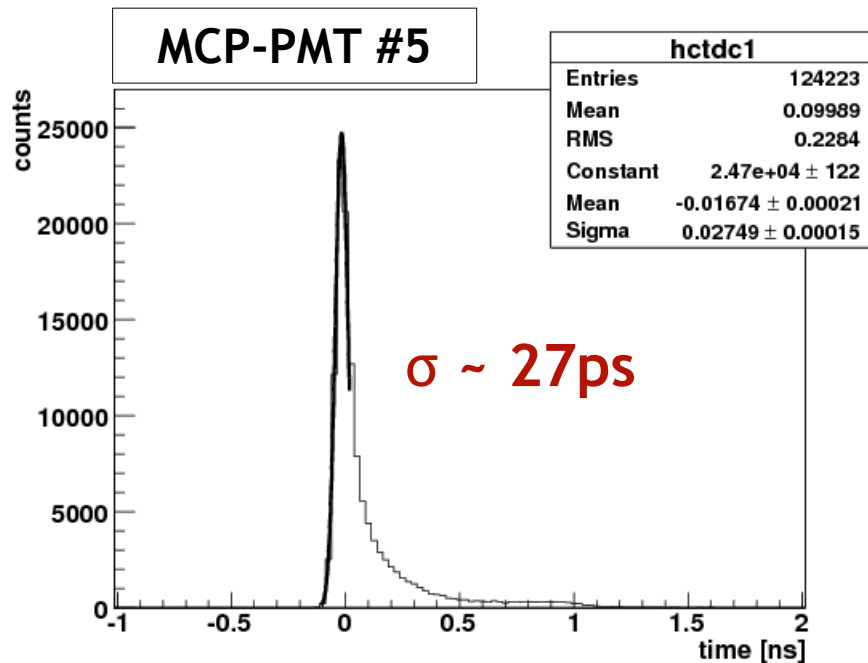


Deconvolution



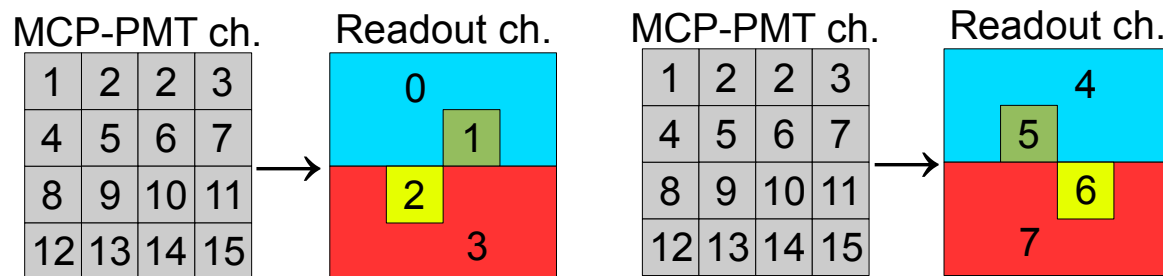
MCP PMT intrinsic timing resolution

- measured with PiLas pico-second laser ($\lambda=406\text{nm}$), attenuated to single photon detection level
- r.m.s. of prompt peak for both samples below 30ps, including contributions from laser ($\sim 15\text{ps}$) and electronics ($\sim 11\text{ps}$)
- intrinsic timing resolution for single photons $\sim 20\text{ps}$
- about $\sim 1\text{ns}$ long tails, mainly due to photoelectron backscattering from front MCP surface



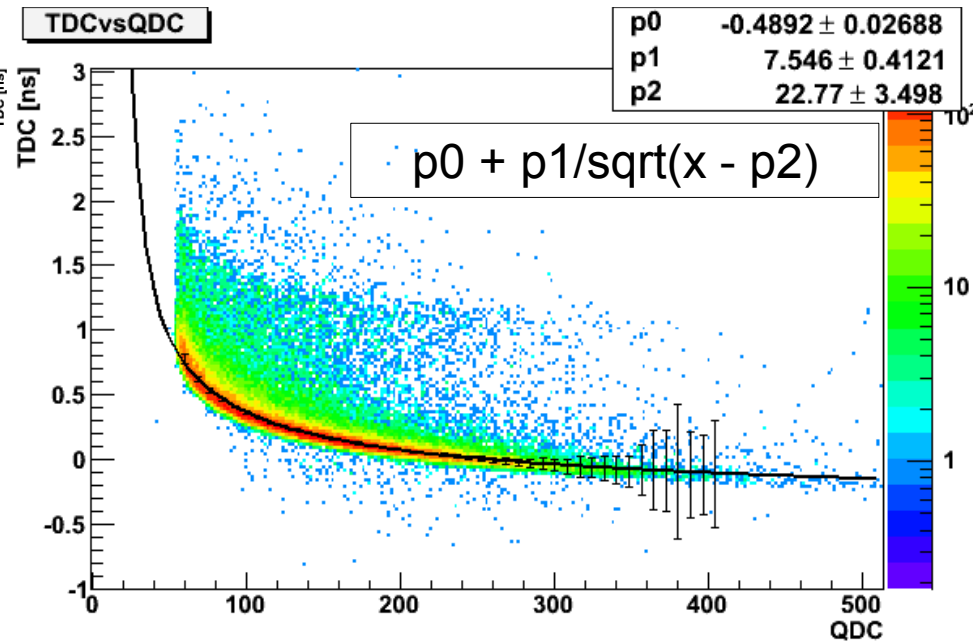
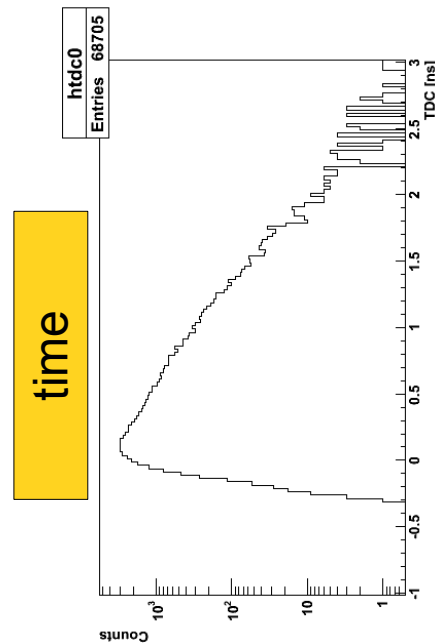
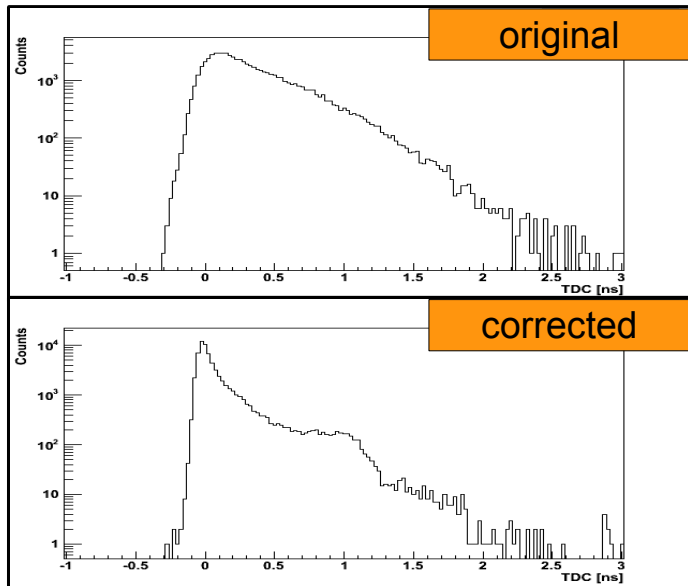
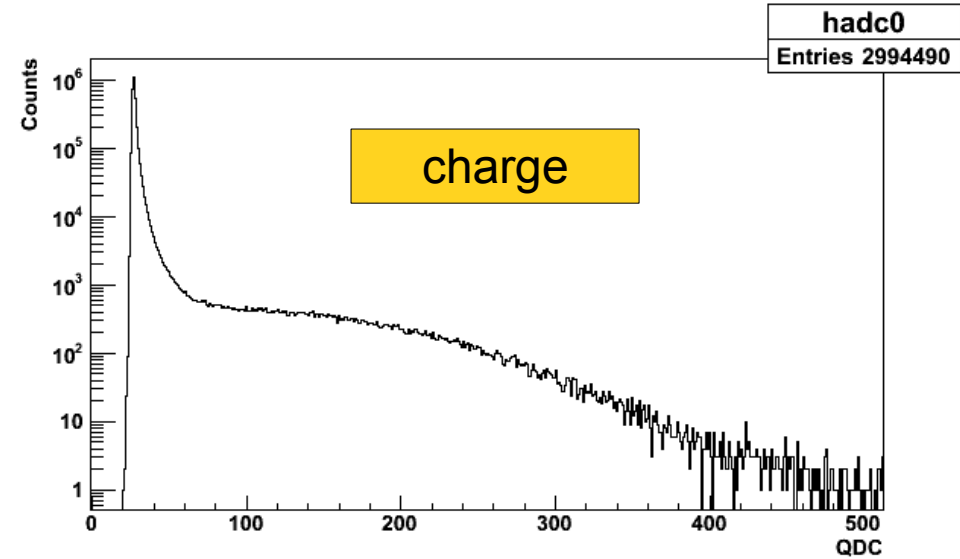
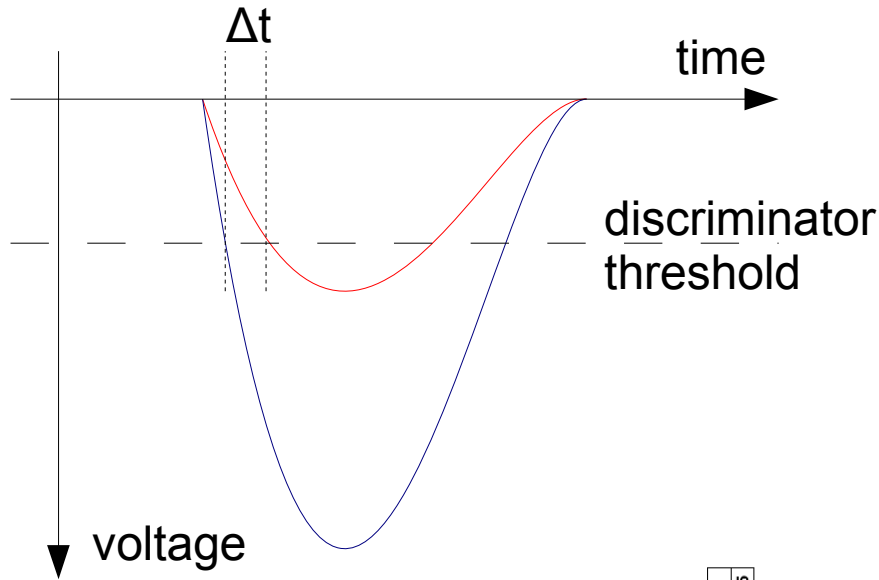
Setup - readout configuration

- Limited number of electronic channels - 4 per MCP-PMT:
- 2 channels near the center instrumented individually
- Remaining channels combined in groups of 7
- Signal from single photon can be detected on more than one channel due to charge sharing, cross-talk ...
- Directly hit channel will most probably have the largest signal.
- Plots labeled 'crosstalk suppressed' use only the channel with the largest signal.



Time-walk correction

- Leading Edge discriminator - triggers at set signal voltage level → smaller pulses register at later time



Black paint (PbF₂)

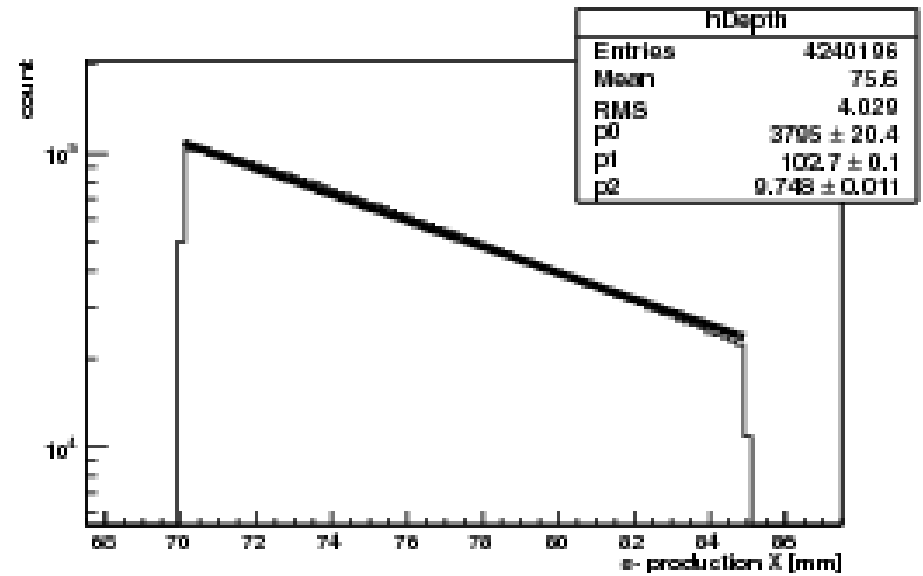
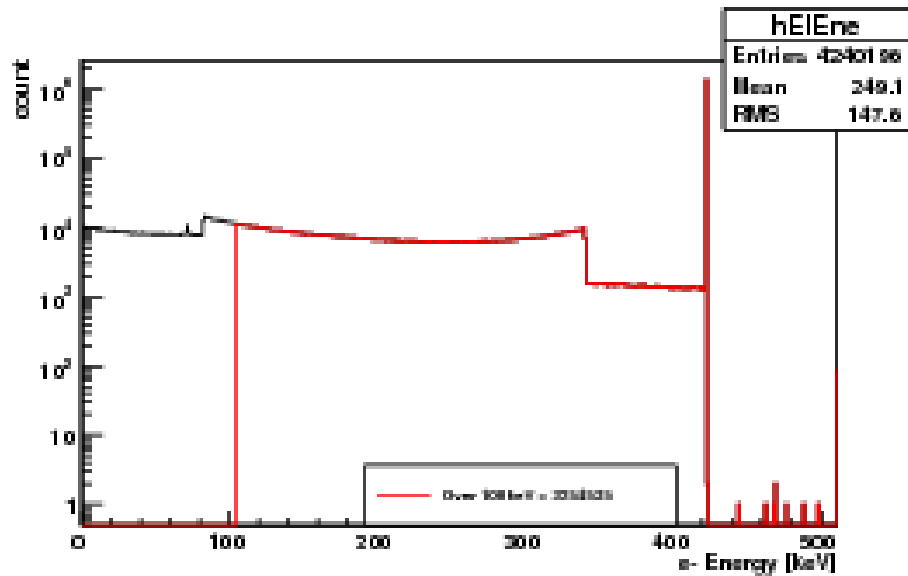
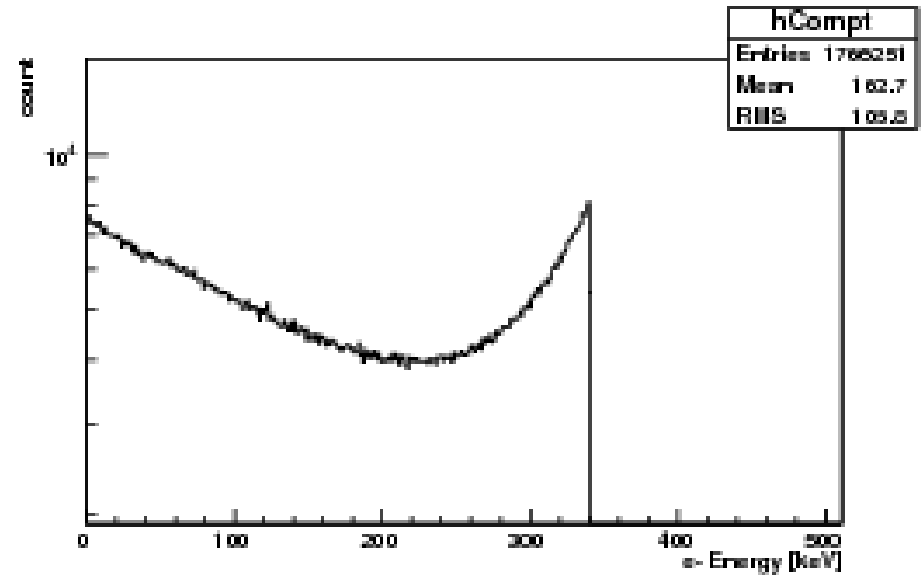
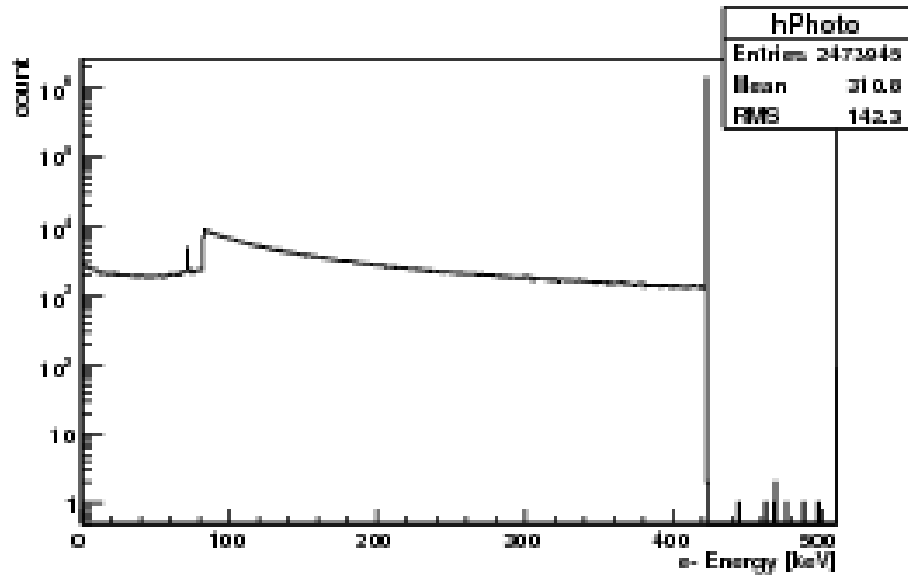
Polished



Ground



Simulation - electron production



Photon interaction with matter

- Compton scattering: γ scatters on electrons, losing part of its energy
 - cross section $\propto Z/E_\gamma$
- photoelectric absorption: γ is absorbed, giving most of its energy to electron
 - cross section $\propto Z^n/E_\gamma^3$, $n \sim 4$

